Optical Lever Based Parylene Cantilevers for Biochemical Sensing

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Abstract: This paper reports the development of optical lever based parylene cantilevers for biochemical sensing. A simple but effective process to fabricate parylene cantilevers using Tetramethylammonium Hydroxide (TMAH) bulkmicromachining was demonstrated. A scheme of using anchoring holes was employed to prevent the peeling off of parylene during TMAH etching. Moreover, ridge structures were incorporated on the cantilever tip to achieve a flat surface for a well-controlled reflected laser spot. An analytical model was presented to guide the design of the cantilever sensor. The stability of the parylene cantilever sensor in water and buffer solution was demonstrated. Based on optical lever method, the parylene cantilevers successfully detected vapour phase alkanethiols, and DNA molecules in buffer solution.

Keywords: Biochemical sensors, cantilevers, parylene, surface stress.

1. INTRODUCTION

Biosensors play crucial roles in disease diagnosis, drug discovery, national security, environment monitoring, food safety, etc. Microfabricated cantilevers have proven to be a promising label-free sensing platform for a large variety of biomolecules [1-4]. Cantilever sensors can operate in either resonant mode (resonant frequency shift) or static mode (static bending). Because of its ability to operate in both liquid and air, the static mode operation is becoming especially attractive [5-19]. The enthusiasm on such kind of sensor is mainly because it has advantages such as label-free detection, simple sensor structure, high sensitivity, etc. The operation principle is schematically illustrated in Fig. (1). One side of the micro-cantilever is first immobilized with a probe or receptor layer (e.g., probe single-stranded DNA). The selective binding of target molecules (e.g., complementary single-stranded DNA) to the immobilized probe layer results in a surface stress change and as a consequence causes a mechanical bending of the cantilever. Therefore, the presence of target molecules can be detected by monitoring the bending of the cantilever. The bending of the cantilever is usually detected by optical lever method as shown in Fig. (1). With this method, the small deflection of the cantilever is converted to a much larger displacement on the position sensitive device by the reflected laser beam.

The displacement of the cantilever tip can be derived from Stoney's equation [20]:



Fig. (1). Schematic presentation of the operating principle of cantilever biosensors. Note the deflection of the cantilever is exaggerated.

$$\Delta y = \frac{3(1-\nu)L^2}{Et^2} \Delta \sigma , \qquad (1)$$

where v is the Poisson's ratio, E is the Young's modulus of cantilever material, t is the cantilever thickness, L is the cantilever length, and $\Delta \sigma$ is the surface stress change caused by the adsorbed molecules. It is apparent that the bending is inversely proportional to the Young's modulus of the cantilever material. So far, the majority of cantilever biosensors are fabricated using solid-state materials such as silicon nitride or silicon. If a softer material is employed, the deflection of cantilever will be more significant and thus the sensitivity will be much higher. Polymer cantilevers using SU-8 and other plastics have been demonstrated [21-24]. This paper reports the development of a cantilever biosensor based on parylene material. Parylene is the generic name for members of a unique family of thermoplastic polymers that are deposited by using the dimer of para-xylylene (di-paraxylylene, or DPXN) [25]. Parylene deposition is a room temperature, highly conformal, vapor phase process.

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Parylene is chemically inert and is not attacked by most wet chemicals. Therefore, we can use wet chemicals such as TMAH (Tetramethylammonium Hydroxide) to fabricate parylene cantilevers with very low cost. There are several members of parylene commonly used, such as parylene N, C, F, and D. Parylene C is chosen as the cantilever material because its deposition rate is fairly high (3~5µm/hour). Parylene C has a Young's modulus of 2.8 GPa, two orders of magnitude smaller than that of silicon nitride.



Fig. (2). Cross-sectional view of a cantilever sensor. The top layer is made of gold and the bottom layer is made of parylene C.

2. THEORETICAL CALCULATIONS

To immobilize the probe layer, a metal layer such as gold is usually coated on the cantilever surface. Therefore, the cantilever sensor should be treated as a composite beam (bimetallic strip), which is composed of two different materials, as shown in Fig. (2). If we assume all the layers have the same width w and length l, the neutral plane of the composite beam locates at [26]:

$$y_c = \frac{\sum_{i} E_i^* t_i y_{ci}}{\sum_{i} E_i^* t_i}$$
(2)

where y_{ci} , t_i and E_i^* are the coordinate of geometry centre, thickness and the modified Young's modulus of the i^{th} layer (i=1, 2), respectively. The modified Young's modulus can be expressed as $E_i^* = \frac{E_i}{1 - v_i}$, where E_i and v_i are the Young's

modulus and Poisson's ratio of the ith layer respectively. The moment of inertia of the ith layer is given by [31]:

$$I_{zi} = \frac{wt_i^3}{12} + (y_c - y_{ci})^2 wt_i$$
(3)

The bending angle of the tip can be written as [32]:

$$\theta = -\frac{\sigma w(y_{top} - y_c)l}{\sum_i E_i^* I_{zi}}$$
(4)

where σ is the surface stress and y_{top} is the coordinate of the top surface (gold). The displacement of the cantilever tip for small bending angle thus can be written as:

$$\Delta y \approx \frac{l}{2} \theta = -\frac{\sigma w (y_{top} - y_c) l^2}{2 \sum_i E_i^* I_{zi}}$$
(5)

If we have only one layer, the above equation will be degenerated to the well-known Stoney's equation. Based on this analytical model, it is observed that the metal layer, although very thin, has a non-negligible impact on the sensitivity of the cantilever. For example, if the parylene is $2.6 \,\mu m$, a 20 nm gold layer may reduce the sensitivity by 45 %.

For such a composite beam, if the temperature increases the beam will bend due to different linear thermal expansion coefficients of the two materials. If the temperature increment is ΔT and linear thermal expansion coefficients for two layers are γ_1 and γ_2 respectively, the tip displacement is given by Eq. 6 [27]. The typical value for the cantilever we used is in the range of 200~300 nm/°C.

$$\Delta y_{t} = \frac{3(\gamma_{2} - \gamma_{1})\Delta T(t_{1} + t_{2})l^{2}}{t_{2}^{2} \left(4 + 6\frac{t_{1}}{t_{2}} + 4\left(\frac{t_{1}}{t_{2}}\right)^{2} + \frac{E_{1}^{*}}{E_{2}^{*}}\left(\frac{t_{1}}{t_{2}}\right)^{3} + \frac{E_{2}^{*}}{E_{1}^{*}}\frac{t_{2}}{t_{1}}\right)}$$
(6)

3. FABRICATION

Parylene cantilevers have been fabricated using surface micromachining previously [28]. In this work a simple and low cost process to fabricate parylene C cantilevers using TMAH bulk-micromachining was demonstrated. A brief fabrication process is described in Fig. (3).



Fig. (3). Process flow of parylene cantilevers.

It has been observed that TMAH does not etch parylene C. However, it attacks the interface between silicon and parylene and peels off parylene films. A scheme of using anchoring holes was employed to prevent the peeling off of parylene C during TMAH etching. Five-inch, (100) siliconwafers were used for the fabrication of our biosensors. The first step was to etch 20-30 µm deep anchor holes in the wafer using Deep Reactive Ion Etching (DRIE). In the second step, 0.5 µm thick oxide layer was grown on the wafer using wet thermal oxidation. In the following step, a parylene C layer with desired thickness was vapour-phase deposited. The parylene C layer was then patterned using Reactive Ion Etching (RIE) with oxygen plasma. The silicon dioxide layer was removed from the openings using Buffered Oxide Etch (BOE). In the next step, TMAH was used to etch silicon, creating the freestanding cantilevers. The silicon underneath the cantilever was removed due to the convex corner undercut [29]. The oxide layer on the bottom surface of the cantilever was then stripped using BOE. Finally, a 20 nm gold layer was evaporated on the surface to provide a functional layer to immobilize DNA. Later the wafer was diced into small chips that were tested in this research.

It is also very interesting to note that after TMAH etching, the Parylene C becomes more hydrophobic. As illustrated in Fig. (4), the contact angle was increased from 70° to 90° .



Fig. (4). Contact angle change on parylene C before (**a**) and after (**b**) 12 hours, 10% TMAH etching.

The SEM picture of two parylene cantilevers coated with a thin gold layer is shown in Fig. (**5a**). The anchoring holes are $50 \ \mu\text{m} \times 50 \ \mu\text{m}$. We found out stiction was a yield issue for this bulk-micromachining process. As shown in Fig. (**5b**), many long cantilevers were pinned to the substrate and the sidewall due to stiction.

This issue can be resolved using diluted TMAH $(5\%\sim10\%)$, which results in very rough etched silicon surface [30]. By using 10% TMAH, the stiction was reduced significantly as shown in Fig (**6a**). The resulted rough silicon

surface is shown in Fig. (**6b**). The longest freestanding cantilever fabricated was 750 μ m. As a comparison, when etched with 25% TMAH, the longest freestanding cantilever was only 350 μ m.

As shown in Fig. (6), the cantilevers fabricated using this technique usually curled up due to stress gradient, making it difficult to obtain a good reflected laser spot from the tip of the cantilever. To address this issue, cantilever tips were integrated with ridge structures, which were formed by filling trenches etched on the cantilever tip areas. The trenches were etched together with the anchoring holes using DRIE in the very first step. Therefore the fabrication process was not complicated. These trenches were 4 μ m wide and 50-100 μ m long and about 20-30 μ m deep. Since parylene coating is conformal, it completely filled the trenches, leading to planarized surfaces for photolithography in the following steps. A brief fabrication process of the new cantilevers is described in Fig. (7).

Fig. (8) shows the SEM pictures of cantilevers with ridges integrated on their tips. It can be observed that the ridges resulted in very flat cantilever tips, which can lead to very good reflected laser spot. It is worth noting that these ridges also help to reduce stiction by reducing contact areas.



Fig. (5). (a) Scanning Electron Microscope (SEM) picture of gold-coated parylene cantilevers. The two cantilevers are 200 μ m wide, 2.2 μ m thick, 100 μ m and 200 μ m long, respectively. (b) SEM pictures of longer cantilevers (720 μ m, 650 μ m, 550 μ m and 450 μ m) sticking to the substrate.



Fig. (6). (a) SEM picture of an array of cantilevers with lengths ranging from a 100 μm to 720 μm. The upward curling of the cantilevers is obvious. **(b)** Rough surface resulted from diluted TMAH etching of silicon.



Fig. (7). Process flow of parylene cantilevers with trenches at the tip.

4. EXPERIMENTAL

A laser diode with fibre pigtail (635 nm wave length, ThorLabs, NJ, USA) was used to measure the deflection of the cantilever. The reflected laser beam from the cantilever was monitored using a PSD (position-sensing device, model name: PSM 2-10, On-trak Photonics Inc, CA, USA). The PSD has a sensing area of 10mm × 10mm and a resolution of 250 nm. The output of the PSD was amplified by position sensing amplifier (OT- 301, On-trak Photonics Inc, CA, USA) and recorded using a DAQ card (PCI - 6250 with 16 bit resolution, National Instruments, Austin, TX, USA). One thousand samples were collected in every second. Every data point was calculated by averaging the 1000 samples within one second. A polysilicon thermistor was used to record the ambient temperature change. In addition, a thermal couple was placed inside the fluid cell to monitor the temperature difference between the solution and ambient. It is worth noting that it is crucial since the solution and the ambient may have different temperatures. The whole setup was enclosed in a black box on a vibration-isolated table to avoid noises from background light and ground vibration. The cantilevers used in experiments have a dimension of 375μ m×200 μ m ×2.65 μ m and are coated with 20 nm gold on the top surface, if not specified.

4.1. Temperature Sensitivity Test

The fluid cell with cantilever sensors was placed on a Peltier heater to measure the temperature sensitivity. The change in the position of the tip of the cantilever along with the change in the temperature of DI water is plotted in Fig. (9). The temperature sensitivity of the parylene cantilever was measured to be ~240 nm/°C. This is comparable to the theoretical bending of the tip of the cantilever (~227 nm/°C) calculated using Eq. 6, assuming coefficients of thermal expansions (CTEs) are 14×10^{-6} /K for gold and 69×10^{-6} /K for parylene. As the temperature increased, the cantilever bent upward because parylene C has a higher thermal coefficient of expansion than gold. It can be observed that the temperature needs to be carefully monitored during the operation in order to detect low concentrations of biomolecules.



Fig. (8). (a) SEM picture of a gold-coated parylene cantilever with two parallel ridges on both sides of the tip. (b) SEM picture of a gold-coated parylene cantilever with rectangular ridge under the tip. The scale bars on figures (a) and (b) are 200 μ m and 100 μ m, respectively.

(a)

(b)



Fig. (9). Temperature sensitivity of a cantilever sensor. 20 nm of gold is coated on the surface of the cantilever.

4.2. Stability of Parylene Cantilever

Stability of parylene cantilevers in DI water was studied. Fig. (10a) shows the cantilever deflection and temperature change of the solution over a period of more than one hour. It can be clearly observed that the displacement of the cantilever follows the same trend as the temperature. As shown in Fig. (10b), after temperature compensation (using the temperature sensitivity measured in section 4.1), the cantilever became very stable with a standard deviation of 3.3 nm.

4.3. Sensitivity to PBS Concentration

We studied the sensitivity of gold-coated parylene cantilevers to PBS concentration. The result of the experiment is shown in Fig. (11). The chip with cantilever sensors was placed in the fluid cell, which was filled completely with DI water. Then the laser was focused on a cantilever and the bending of the cantilever was monitored using a Photo Sensing Diode (PSD). DI water and PBS solution with a concentration of 1X were injected into the fluid cell in turn. Two consecutive injections were separated by 12 minutes. The ambient temperature measured by the polysilicon piezoresistor and the temperature difference between the solution and ambient are in Fig. (11a). This result clearly shows that the ambient temperature and solution temperature are not necessarily same. The displacement of the cantilever was monitored by the PSD and shown in Fig. (11b). The temperature of the solution is also plotted in Fig. (11b), by combining results of polysilicon thermistor and thermal couple together. The temperature-compensated displacement is shown in Fig. (11c). From this experiment, we found that the displacement of gold-coated parylene cantilever caused by the change of buffer concentration is negligible after temperature compensation. This result again signifies the importance of monitoring the solution temperature in situ. It is worth noting that this conclusion will not be valid if the cantilever surface is immobilized with some biomolecules such as DNA.

4.4. Alkanethiol Test

A cantilever sensor $(250\mu m \times 200\mu m \times 1.65 \mu m)$ was placed in an empty fluid cell (5 ml in volume) and the laser was focused on the tip to obtain a base line for about 50 minutes. Then 3 drops of 1-Octanethiol (98.5+%, Sigma-Aldrich Inc, Mo, USA) were injected in the fluid cell. The volatile alkanethiol evaporated and immobilized on the gold surface, inducing surface stress on the cantilever. The recorded data for the displacement of the tip of the cantilever is shown in Fig. (12). According to the data recorded, the tip of the cantilever bends about 165 nm downwards (away form the gold surface). This bending corresponds to a compressive surface stress of about 0.030 N/m according to Eq. 5. The surface stress induced falls within the range reported in the literature (0.001-0.250 N/m depending on the alkanethiol carbon chain length and magnitude of surface coverage) [24].

The test was repeated with water drops instead of alkanethiol. The response of the gold-coated cantilever for the absorption of the water vapours is shown in Fig. (13). It can be clearly seen that there was no change in the position of the cantilever tip when water drops were added in the fluid cell. This further confirms that the displacement in Fig. (12) was caused by the alkanethiol molecules.



Fig. (10). (a) Temperature change and cantilever displacement versus time. (b) Temperature-compensated cantilever displacement.



Fig. (11). The sensitivity of a parylene cantilever to the concentration of PBS. (a) Ambient temperature measured by polysilicon thermistor and the temperature difference between the solution and ambient measured by thermocouple. (b) Displacement of the cantilever tip and the temperature change of the solution when it was switched between DI water and 1X PBS. (c) Displacement of the cantilever tip after temperature-compensation.



Alkanethiol Test

Fig. (12). Data showing the sensitivity of cantilever sensor to alkanethiol.

4.5. DNA Test

40-nt-long ssDNA nucleotide was used as the probe molecule (Synthegen, Florida). The sequence for the probe ssDNA molecule was 5'-TTAAGGTCTGGACTGGCCTG AATTTAGCGCCAGCTTACTG-3' and the sequence of the complementary target ssDNA was 3'-CAGACCTGACCG GAC-5' [14]. A parylene cantilever (250μ m× 200μ m× 2.2μ m) was placed in the fluid cell and flushed with buffer solution. The probe molecules were mixed with the buffer solution and injected into the fluid cell (~8 μ M). The deflection of the cantilever tip is shown in Fig. (14). According to the data recorded, the cantilever bent about 215 nm downwards (away from the gold surface). This shows a higher sensitivity of the parylene cantilever compared to its silicon nitride counterparts [14]. This bending corresponds to a compressive surface stress of about 0.040 N/m according to Eq. 5.

Alkanethiol Test Repeated with Water



Fig. (13). Data showing the stability of cantilever sensor when water is injected instead of alkanethiol. The peak is the point when water drop was injected in the fluid cell.



Immobalization of ssDNA

Fig. (14). The deflection of a parylene cantilever sensor ($250\mu m \times 200\mu m \times 2.2\mu m$) to the ssDNA immobilization on gold surface.

After 40 minutes, the fluid cell was flushed with the buffer solution. The target molecules were then mixed with the buffer solution ($\sim 3.75 \mu$ M) and injected into the fluid cell. Again, the deflection of the cantilever tip was monitored using the optical lever. The response of the parylene cantilever during the hybridization of complementary target ssDNA is shown in Fig. (15). According to the recorded data, the cantilever bent about 75 nm upwards (towards the gold surface). This means that hybridization reduces the compressive stress induced by the immobilization. This observation is consistent with the result reported in [14]. The 75 nm bending corresponds to a reduction in compressive surface stress of about 0.014 N/m according to Eq. 5, leading to a sensitivity of 5.4 nm/(mN/m). This again shows a higher tip displacement sensitivity of the parylene cantilever compared to its silicon nitride counterparts [14].

CONCLUSION

This paper presents development of parylene cantilever sensors. Parylene cantilevers were successfully fabricated using low-cost TMAH bulk-micromachining. Ridges were integrated to make flat cantilever tips for better reflected laser spots. The bimaterial cantilever sensor was stable in water and PBS, but was very sensitive to temperature. The high sensitivity of parylene cantilevers was demonstrated by alkanethiols and DNA sensing. The parylene cantilever shows a promising future as a powerful tool for the detection of chemicals and macro biomolecules.

Hybridization of ssDNA



Fig. (15). The response of the cantilever sensor during the hybridization of target ssDNA with the probe ssDNA immobilized on the gold surface of the cantilever sensor.

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